Memory Hierarchy Requirements

• Allow multiple processes to simultaneously occupy memory and provide *protection*
  – Don’t let programs read from or write to each other’s memories

• Give each program the illusion that it has its own *private address space* (via *translation*)
  – Suppose code starts at address 0x00400000, then different processes each think their code resides at the same address
  – Each program must have a *different* view of memory
Goals of Virtual Memory

• Next level in the memory hierarchy
  – Provides illusion of very large main memory
  – Working set of “pages” residing in main memory
    (subset of all pages residing on disk)

• Main goal: Avoid reaching all the way back to disk as much as possible

• Additional goals:
  – Let OS share memory among many programs and protect them from each other
  – Each process thinks it has all the memory to itself
Review: Paging Terminology

• Programs use *virtual addresses (VAs)*
  – Space of all virtual addresses called *virtual memory (VM)*
  – Divided into pages indexed by *virtual page number (VPN)*

• Main memory indexed by *physical addresses (PAs)*
  – Space of all physical addresses called *physical memory (PM)*
  – Divided into pages indexed by *physical page number (PPN)*
Virtual Memory Mapping Function

• How large is main memory? Disk?
  – Don’t know! Designed to be interchangeable components
  – Need a system that works regardless of sizes

• Use lookup table (page table) to deal with arbitrary mapping
  – Index lookup table by # of pages in VM
    (not all entries will be used/valid)
  – Size of PM will affect size of stored translation
Address Mapping

• Pages are aligned in memory
  – Border address of each page has same lowest bits
  – Page size is same in VM and PM, so denote lowest
    \( O = \log_2(\text{page size/byte}) \) bits as *page offset*

• Use remaining upper address bits in mapping
  – Tells you which page you want (similar to Tag)

__Diagram:__

- **Physical Page #** | **Page Offset**
- **Virtual Page #** | **Page Offset**

- Not necessarily the same size
- Same Size
Address Mapping: Page Table

• **Page Table functionality:**
  – Incoming request is Virtual Address (VA), want Physical Address (PA)
  – Physical Offset = Virtual Offset (page-aligned)
  – So just swap Virtual Page Number (VPN) for Physical Page Number (PPN)

• **Implementation?**
  – Use VPN as index into PT
  – Store PPN and management bits (Valid, Access Rights)
  – Does NOT store actual data (the data sits in PM)
Virtual Address: [VPN, offset]

1) Index into PT using VPN

Page Table

<table>
<thead>
<tr>
<th>V</th>
<th>AR</th>
<th>PPN</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X</td>
<td>XX</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

2) Check Valid and Access Rights bits

3) Concatenate PPN and offset

PPN [offset]

Physical Address

4) Use PA to access memory
Page Table Entry Format

• Contains either PPN or indication not in main memory

• **Valid** = Valid page table entry
  – 1 → virtual page is in physical memory
  – 0 → OS needs to fetch page from disk

• **Access Rights** checked on every access to see if allowed (provides protection)
  – *Read Only*: Can read, but not write page
  – *Read/Write*: Read or write data on page
  – *Executable*: Can fetch instructions from page
Page Tables (1/2)

• A page table (PT) contains the mapping of virtual addresses to physical addresses

• Page tables located in main memory – Why?
  – Too large to fit in registers \((2^{20}\) entries for 4 KiB pages)
  – Faster to access than disk and can be shared by multiple processors

• The OS maintains the PTs
  – Each process has its own page table
    • “State” of a process is PC, all registers, and PT
  – OS stores address of the PT of the current process in the \textit{Page Table Base Register}
Page Tables (2/2)

- **Solves fragmentation problem**: all pages are the same size, so can utilize all available slots
- OS must reserve "swap space" on disk for each process
  - Running programs requires hard drive space!
- To grow a process, ask Operating System
  - If unused pages in PM, OS uses them first
  - If not, OS swaps some old pages (LRU) to disk
Paging/Virtual Memory Multiple Processes

User A:
Virtual Memory

- Code
- Static
- Code

Page Table A

Physical Memory

64 MB

User B:
Virtual Memory

- Stack
- Page Table B
- Static
- Code

Page Table B
Question: How many bits wide are the following fields?

• 16 KiB pages
• 40-bit virtual addresses
• 64 GiB physical memory

<table>
<thead>
<tr>
<th></th>
<th>VPN</th>
<th>PPN</th>
</tr>
</thead>
<tbody>
<tr>
<td>A)</td>
<td>26</td>
<td>26</td>
</tr>
<tr>
<td>B)</td>
<td>24</td>
<td>20</td>
</tr>
<tr>
<td>C)</td>
<td>22</td>
<td>22</td>
</tr>
<tr>
<td>D)</td>
<td>26</td>
<td>22</td>
</tr>
</tbody>
</table>
Retrieving Data from Memory

1) Access page table for address translation

2) Access correct physical address

Requires two accesses of physical memory!
Virtual Memory Problem

• 2 physical memory accesses per data access = SLOW!

• Build a separate cache for the Page Table
  – For historical reasons, cache is called a Translation Lookaside Buffer (TLB)
  – Notice that what is stored in the TLB is NOT data, but the VPN → PPN mapping translations
TLBs vs. Caches

- TLBs usually small, typically 16 – 512 entries
- TLB access time comparable to cache (« main memory)
- TLBs can have associativity
  - Usually fully/highly associative
Where Are TLBs Located?

- Which should we check first: Cache or TLB?
  - Can cache hold requested data if corresponding page is not in physical memory? No
  - With TLB first, does cache receive VA or PA?

Notice that it is now the TLB that does translation, not the Page Table!
Address Translation Using TLB

Virtual Address

VPN

TLB

VPN

TLB Tag  TLB Index  Page Offset

Tag  PPN

(used just like in a cache)

PA split two different ways!

PPN  Page Offset

Tag  Index  Offset

Data Cache

Tag  Block Data

...
Typical TLB Entry Format

<table>
<thead>
<tr>
<th>Valid</th>
<th>Dirty</th>
<th>Ref</th>
<th>Access Rights</th>
<th>TLB Tag</th>
<th>PPN</th>
</tr>
</thead>
<tbody>
<tr>
<td>X</td>
<td>X</td>
<td>X</td>
<td>XX</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

- **Valid** and **Access Rights**: Same usage as previously discussed for page tables
- **Dirty**: Basically always use write-back, so indicates whether or not to write page to disk when replaced
- **Ref**: Used to implement LRU
  - Set when page is accessed, cleared periodically by OS
  - If Ref = 1, then page was referenced recently
- **TLB Index**: VPN mod (# TLB sets)
- **TLB Tag**: VPN – TLB Index
Question: How many bits wide are the following?

- 16 KiB pages
- 40-bit virtual addresses
- 64 GiB physical memory
- 2-way set associative TLB with 512 entries

<table>
<thead>
<tr>
<th>Valid</th>
<th>Dirty</th>
<th>Ref</th>
<th>Access Rights</th>
<th>TLB Tag</th>
<th>PPN</th>
</tr>
</thead>
<tbody>
<tr>
<td>X</td>
<td>X</td>
<td>X</td>
<td>XX</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>TLB Tag</th>
<th>TLB Index</th>
<th>TLB Entry</th>
</tr>
</thead>
<tbody>
<tr>
<td>A) 12</td>
<td>14</td>
<td>38</td>
</tr>
<tr>
<td>B) 18</td>
<td>8</td>
<td>45</td>
</tr>
<tr>
<td>C) 14</td>
<td>12</td>
<td>40</td>
</tr>
<tr>
<td>D) 17</td>
<td>9</td>
<td>43</td>
</tr>
</tbody>
</table>
Fetching Data on a Memory Read

1) Check TLB (input: VPN, output: PPN)
   - **TLB Hit**: Fetch translation, return PPN
   - **TLB Miss**: Check page table (in memory)
     - **Page Table Hit**: Load page table entry into TLB
     - **Page Table Miss (Page Fault)**: Fetch page from disk to memory, update corresponding page table entry, then load entry into TLB

2) Check cache (input: PPN, output: data)
   - **Cache Hit**: Return data value to processor
   - **Cache Miss**: Fetch data value from memory, store it in cache, return it to processor
Page Faults

• Load the page off the disk into a free page of memory
  – Switch to some other process while we wait

• Interrupt thrown when page loaded and the process' page table is updated
  – When we switch back to the task, the desired data will be in memory

• If memory full, replace page (LRU), writing back if necessary, and update both page table entries
  – Continuous swapping between disk and memory called “thrashing”
Performance Metrics

• VM performance also uses Hit/Miss Rates and Miss Penalties
  – *TLB Miss Rate:* Fraction of TLB accesses that result in a TLB Miss
  – *Page Table Miss Rate:* Fraction of PT accesses that result in a page fault

• Caching performance definitions remain the same
  – Somewhat independent, as TLB will always pass PA to cache regardless of TLB hit or miss
• Are the following scenarios for a single data access possible?
  – TLB Miss, Page Fault  
    Yes
  – TLB Hit, Page Table Hit  
    No
  – TLB Miss, Cache Hit  
    Yes
  – Page Table Hit, Cache Miss  
    Yes
  – Page Fault, Cache Hit  
    No
**Question:** A program tries to load a word at X that causes a TLB miss but not a page fault. Are the following statements TRUE or FALSE?

1) The page table does not contain a valid mapping for the virtual page corresponding to the address X

2) The word that the program is trying to load is present in physical memory

<table>
<thead>
<tr>
<th></th>
<th>1</th>
<th>2</th>
</tr>
</thead>
<tbody>
<tr>
<td>A)</td>
<td>F</td>
<td>F</td>
</tr>
<tr>
<td>B)</td>
<td>F</td>
<td>T</td>
</tr>
<tr>
<td>C)</td>
<td>T</td>
<td>F</td>
</tr>
<tr>
<td>D)</td>
<td>T</td>
<td>T</td>
</tr>
</tbody>
</table>
VM Performance

• Virtual Memory is the level of the memory hierarchy that sits *below* main memory
  – TLB comes *before* cache, but affects transfer of data from disk to main memory
  – Previously we assumed main memory was lowest level, now we just have to account for disk accesses

• Same CPI, AMAT equations apply, but now treat main memory like a mid-level cache
Typical Performance Stats

Caching
- cache entry
- cache block (≈32 bytes)
- cache miss rate (1% to 20%)
- cache hit (≈1 cycle)
- cache miss (≈100 cycles)

Demand paging
- page frame
- page (≈4Ki bytes)
- page miss rate (<0.001%)
- page hit (≈100 cycles)
- page miss (≈5M cycles)
Impact of Paging on AMAT (1/2)

• Memory Parameters:
  – L1 cache hit = 1 clock cycles, hit 95% of accesses
  – L2 cache hit = 10 clock cycles, hit 60% of L1 misses
  – DRAM = 200 clock cycles (≈100 nanoseconds)
  – Disk = 20,000,000 clock cycles (≈10 milliseconds)

• Average Memory Access Time (no paging):
  – $1 + 5\% \times 10 + 5\% \times 40\% \times 200 = 5.5$ clock cycles

• Average Memory Access Time (with paging):
  – $5.5$ (AMAT with no paging) + ?
Impact of Paging on AMAT (2/2)

- Average Memory Access Time (with paging) =
  - $5.5 + 5\% \times 40\% \times (1 - \text{HR}_{\text{Mem}}) \times 20,000,000$

- AMAT if $\text{HR}_{\text{Mem}} = 99\%$?
  - $5.5 + 0.02 \times 0.01 \times 20,000,000 = 4005.5$ (≈728x slower)
  - 1 in 20,000 memory accesses goes to disk: 10 sec program takes 2 hours!

- AMAT if $\text{HR}_{\text{Mem}} = 99.9\%$?
  - $5.5 + 0.02 \times 0.001 \times 20,000,000 = 405.5$

- AMAT if $\text{HR}_{\text{Mem}} = 99.9999\%$
  - $5.5 + 0.02 \times 0.000001 \times 20,000,000 = 5.9$
Impact of TLBs on Performance

• Each TLB miss to Page Table ~ L1 Cache miss
• **TLB Reach**: Amount of virtual address space that can be simultaneously mapped by TLB:
  – TLB typically has 128 entries of page size 4-8 KiB
  – $128 \times 4 \text{ KiB} = 512 \text{ KiB} = \text{just 0.5 MiB}$
• What can you do to have better performance?
  – Multi-level TLBs [Conceptually same as multi-level caches]
  – Variable page size (segments)
  – Special situationally-used “superpages” [Not covered here]
Aside: Context Switching

• How does a single processor run many programs at once?

• *Context switch:* Changing of internal state of processor (switching between processes)
  – Save register values (and PC) and change value in Page Table Base register

• What happens to the TLB?
  – Current entries are for different process
  – Set all entries to invalid on context switch
Virtual Memory Summary

• User program view:
  – Contiguous memory
  – Start from some set VA
  – “Infinitely” large
  – Is the only running program

• Reality:
  – Non-contiguous memory
  – Start wherever available memory is
  – Finite size
  – Many programs running simultaneously

• Virtual memory provides:
  – Illusion of contiguous memory
  – All programs starting at same set address
  – Illusion of ~ infinite memory
    (2^{32} or 2^{64} bytes)
  – Protection, Sharing

• Implementation:
  – Divide memory into chunks (pages)
  – OS controls page table that maps virtual into physical addresses
  – memory as a cache for disk
  – TLB is a cache for the page table